Signal Propagation in Transmission Lines with Losses Using Fibonacci Wave Functions

Simon Hissem and Lamine Mamadou Doumbia

Abstract — In this paper, the general model for an infinite LC ladder network using Fibonacci wave functions that were applied to lossless transmission lines will be extended to transmission lines including losses. The general model that was derived from a first order system transfer function representing a simple RC or RL circuit will be used to model and analyze transmission lines presenting losses. The LC ladder network model can be applied to any order for each inductor current with its parasitic \( r_L \) resistor and for each capacitor voltage with its parasitic \( r_C \) resistor. The extension of the proposed general model to transmission lines with losses is subject to Heaviside condition for both resistors \( r_C \) and \( r_L \).

Keywords — Fibonacci wave functions, Heaviside, LC ladder, losses, Pascal’s triangle, Transmissions lines.

I. INTRODUCTION

In the previous papers [1] and [2], Fibonacci wave functions (FWFs) were introduced to model an infinite LC ladder network without losses. A general model for any LC ladder network order was also introduced.

In the literature, very few papers analyzed either LC ladder or transmission cable including losses with exhaustive mathematical calculations [4]. Most other papers used only lossless modeling and analysis. Introducing losses in such systems leads to another level of difficulties in modelling and analyzing these systems [3], [5] and [6]. Fibonacci wave functions may help simplify and extend the analysis to another horizon.

In this paper, the extension of FWFs with its general model to LC ladder network with losses to model a transmission line with resistive losses will be modeled and analyzed for different orders and will be compared to MATLAB-Simulink LC model presenting the same losses. The paper is organized as follow. Sections II and III are dedicated to the general model extension to resistive-capacitive including losses Fibonacci electrical circuit (RC-FEC-Losses) and resistive inductive including losses Fibonacci electrical circuit (RL-FEC-Losses). Section IV describes a comparative study of FWFs and RC-FEC-Losses using MATLAB-Simulink model. Section V shows a comparative study of FWFs and RC-FEC-Losses of transmission line with short and open terminations.

II. RC-FEC-LOSSES FIBONACCI ELECTRICAL CIRCUIT

The original Fibonacci transfer function has the following form [1].

\[
\mathcal{G}_1^{(k,x)}(s) = \frac{K}{s + x_c} \quad (1)
\]

with

\[
K = \omega_1^2 \text{ and } x_c = \frac{1}{RC}
\]

The first order electrical circuit RC-FEC-Losses is presented in Fig. 1.

Fig. 1. First order RC-FEC-Losses.

The equivalent impedance between the capacitor \( C \) and its parasitic resistor \( r_c \) can be easily calculated as follows.

\[
Z_c = \frac{1}{\frac{1}{r_c} + \frac{1}{sC}}
\]

with \( a = \frac{1}{r_c} \) and changing Laplace variable \( s \) to the new reference \( S = s + a \). The impedance \( Z_c \) becomes.

\[
Z_c = \frac{1}{\frac{1}{s} + \frac{1}{sC}}
\]

Furthermore, the circuit in figure 1 can easily be written in the new Laplace reference defined by Laplace variable \( S \)

\[
\frac{V_o}{I_i} = \frac{1}{S} + \frac{1}{S + \frac{1}{RL}} = L \frac{1}{S + \frac{1}{RL}} = L \frac{K}{S + x_c} = L \mathcal{G}_i^{(k,x,a)}(S)
\]

(2)

The second order RC-FEC-Losses circuit diagram shown in Fig. 2 and its transfer function in (3).
The equivalent impedance between the inductor L and its parasitic resistor $r_L$ can be easily calculated as follows:

$$Z_L = r_L + sL = \left(\frac{r_L}{L}\right)L$$

with $a_L = \frac{r_L}{L}$ and changing Laplace variable to the new reference $S = s + a_L$ with the condition $a_L = a$ which is exactly the known Heaviside condition for no signal distortion through the transmission lines. This condition does not eliminate losses through the lines. This condition is necessary to extend the Fibonacci wave functions to transmission lines that present losses.

$$a = \frac{r_L}{L} = \frac{1}{rC} \text{ with } S = s + a \quad (3)$$

The impedance $Z_L$ becomes $Z_L = SL$.

Furthermore, the circuit in figure 2 can easily be written in the new Laplace reference defined by Laplace variable $S_q$.

$$V_1 = \left(L g_1(k_{x,a})(S) + SL\right) V_0 = \frac{L}{C} \left(S + g_1(k_{x,a})(S)\right) V_0$$

$$\frac{I_0}{CV_1^2} = \frac{K}{S + K} = G_2(k_{x,a})(S) \quad (4)$$

The transfer function of the third order RC-FEC-Losses (5) is derived from circuit diagram presented in Fig. 3.

$$I_1 = \left(C g_2(k_{x,a})(S) + SC\right) V_0 = \frac{LC}{L} \left(S + g_2(k_{x,a})(S)\right) V_0$$

$$\frac{V_0}{L_3} = \frac{K}{S + K} = G_3(k_{x,a})(S) \quad (5)$$

One can see that an even $n^{th}$ order RC-FEC-Losses (Fig. 4) will have voltage as input and current as output.

$$n = n_e + n_L \quad (6)$$

$n_c$ total number of capacitors in the circuit.

The FWF of the $n^{th}$ even order of the circuit in Fig. 4 is:

$$\left(\frac{I_0}{CV_1^2}\right)^n = \frac{K}{S + G_n^{(k_{x,a})}(S)} = G_n^{(k_{x,a})}(S) \quad (7)$$

For the $n^{th}$ odd order in the circuit in Fig. 5, the FWF is:

$$\left(\frac{V_0}{L_3} \right)^n = \frac{K}{S + G_n^{(k_{x,a})}(S)} = G_n^{(k_{x,a})}(S) \quad (8)$$

Table I shows general FWFs in RC-FEC-Losses for all orders.

**Table I: RC-FEC-Losses Fibonacci Wave Functions in Reference**

<table>
<thead>
<tr>
<th>$L(S,a)$</th>
<th>$V_0$</th>
<th>$I_0$</th>
<th>$V_0$</th>
<th>$I_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$G_2^{(k_{x,a})}(S)$</td>
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All currents through each inductor and voltages through each capacitor are determined by their corresponding FWFs. For \( n^{th} = 40 \) of RC-FEC-Losses in Fig. 6, its general model can be easily generated with all FWFs for all currents in each inductor and all voltages in each capacitors in Fig. 7.

Fig. 6. \( n^{th} \) even order RC-FEC-Losses.

Fig. 7. \( n^{th} = 40 \) even order RC-FEC-Losses Model using FWFs for each current and voltage branch in reference \( L(S, \alpha) \).

\[ V_o = \frac{K}{S + \frac{K}{x_L}} = g_2^{(k,x_L)}(S) \]  

(10)

The third order RL-FEC-Losses will be defined with an input voltage and output current (Fig. 10) and its FTF in (11).

Fig. 10. First order RL-FEC-Losses.

\[ \frac{I_o}{CV_L} = \frac{K}{S + \frac{K}{x_L}} = g_3^{(k,x_L)}(S) \]  

(11)

An even \( n^{th} \) order RL-FEC-Losses in figure 11 has its FWF expressed in (13).

\[ n = n_c + n_L \]  

(12)

\( n_c \) is the total number of capacitors in the circuit. 
\( n_L \) is the total number of inductance in the circuit.

Fig. 11. \( n^{th} \) even order RL-FEC-Losses.

\[ V_o = \frac{K}{S + g_{n-1}^{(k,x_L)}} = g_n^{(k,x_L)}(S) \]  

(13)

An odd \( n^{th} \) order RL-FEC-Losses in Fig. 12 has its FWF expressed in (14).

Fig. 12. \( n^{th} \) odd order RL-FEC-Losses.

\[ \frac{I_o}{CV_L} = \frac{K}{S + g_{n-1}^{(k,x_L)}} = g_n^{(k,x_L)}(S) \]  

(14)

Table II shows FWFs in the case of RL-FEC-Losses with losses.

III. RL-FEC-LOSES FIBONACCI ELECTRICAL CIRCUIT

As RC-FEC-Losses Fibonacci wave functions FWFs, RL-FEC-Losses can be calculated easily. The first order circuit in Fig. 8 and its FWF is presented in (9).

Fig. 8. First order RL-FEC-Losses.

\[ \frac{I_o}{CV_L} = \frac{K}{S + x_L} = g_1^{(k,x_L)}(S) \]  

(9)

\[ K = \frac{1}{LC} \text{ and } x_L = \frac{R}{L} \]

\[ K = \frac{1}{LC} \]

For the 2\(^{nd} \) order RL-FEC-Losses the FWF is expressed in (10).

Fig. 9. Second order RL-FEC-Losses.

\[ \frac{V_o}{V_L} = \frac{K}{S + g_{n-1}^{(k,x_L)}} = g_n^{(k,x_L)}(S) \]  

(13)
TABLE II: RL-FEC-LOSES FIBONACCI WAVE FUNCTIONS IN REFERENCE $L(S, a)$

<table>
<thead>
<tr>
<th>$n$ even</th>
<th>$n$ odd</th>
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</thead>
<tbody>
<tr>
<td>$\frac{V_1}{V_1} = G_1(Kx, a)$</td>
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</tr>
<tr>
<td>$= \frac{K}{S + x_L}$</td>
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</tbody>
</table>

All currents through each inductor and voltages through each capacitor are determined by their corresponding FWFs. For $n = 40$ of RL-FEC-Loses in Fig. 13, its general model generated with all FWFs for all currents in each inductor and all voltages in each capacitor in Fig. 14.

IV. COMPARATIVE SIMULATION OF RC-FEC-LOSES AND THEIR FWFs

Comparative simulation studies were conducted between the electrical circuits using MATLAB-Simulink model with Fibonacci wave functions for each order in Table I. The studies confirm that these electrical LC ladder circuits for different orders representing different transmission lines length with losses defined by $r_l$ and $r_C$ follow the same recurrent Fibonacci sequence modelled by FWFs [1].

Case 1: $R=1\Omega$; $L=1H$; $C=1F$; $r_l = 0.02\Omega$; $r_C = \frac{1}{k_{rC}} = 50\Omega$

In this case $(K, x_o, a) = (1,1,0.2)$, Pascal’s Triangle in Table II presented in [1] will be used to determine all FWFs. $G_{14}(Kx, a(S))$ taken as an even function, using its numerator and denominator coefficients are expressed in (15) using Table II in reference $L(S, a)$.

$$\frac{I_0}{V_1} = G_14(Kx, a(S)) = \frac{K}{S + x_L}$$

$$\frac{I_0}{V_1} = G_14(Kx, a(S)) = \frac{K}{S + x_L}$$

$$(15)$$

where $K = 15^{14} + 11x_1S^{15} + 12Kx_1S^{10}$

- $55K^3S^6 + 45K^2x_2S^9 + 120K^2S^7$

- $84K^5x_2S^6 + 126K^4S^7 + 70K^4S^8$

- $56K^6S^7 + 21K^5S^8 + 7K^6S^9$

$+ 10Kx_3S^{10}$

Using input voltage $V_i(t) = \alpha$ for all even orders FWFs and input current $I_i(t) = \alpha$ for all odd orders FWFs. Fig. 15 shows the block diagram in both references $L(s)$ and $L(S, a)$ for voltage as input, the figure is also applicable when the input is current. Simulation will be used in $L(S, a)$ since all FWFs are perfectly known.

**Fig. 13.** $n^{th}$ even order RL-FEC-Loses.

**Fig. 14.** $n^{th}$ even order RL-FEC-Loses Model using FWFs for each current and voltage branch in reference $L(S, a)$.

**Fig. 15.** FWFs block diagram in Laplace $L(s)$ & $L(S, a)$. 

**TABLE III: PASCAL’S TRIGRAM GENERAL FORM WITH MULTIPLICATION COEFFICIENTS**

Using input voltage $V_i(t) = \alpha$ for all even orders FWFs and input current $I_i(t) = \alpha$ for all odd orders FWFs. Fig. 15 shows the block diagram in both references $L(s)$ and $L(S, a)$ for voltage as input, the figure is also applicable when the input is current. Simulation will be used in $L(S, a)$ since all FWFs are perfectly known.

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**TABLE III: PASCAL’S TRIGRAM GENERAL FORM WITH MULTIPLICATION COEFFICIENTS**
This block diagram is also applicable for all odd orders FWFs with current as input and voltage as output.

Simulations of $G_{40}(1,1,0.2) = C \cdot G_{40}(1,1,0.2) \cdot (S)$ model and RC-FEC-losses Simulink model for order 40 shown in figure 16 are identical with input voltage $V_i(t) = \alpha = 1V$.

\[
\begin{align*}
I_{L_1}^{(K_x,a)}(K_x,a) &= g_1^{(K_x,a)}(a) \\
V_{L_1}^{(K_x,a)}(K_x,a) &= G_1^{(K_x,a)}(a) = \frac{K}{a + 1 + x_c}
\end{align*}
\]

\[
\begin{align*}
I_{L_2}^{(K_x,a)}(K_x,a) &= g_2^{(K_x,a)}(a) \\
V_{L_2}^{(K_x,a)}(K_x,a) &= G_2^{(K_x,a)}(a) = \frac{K(a + Kx_c)}{1a^2 + 1x_ca + 1K}
\end{align*}
\]

\[
\begin{align*}
I_{L_3}^{(K_x,a)}(K_x,a) &= g_3^{(K_x,a)}(a) \\
V_{L_3}^{(K_x,a)}(K_x,a) &= G_3^{(K_x,a)}(a) = \frac{K(a^2 + Kx^2_c + K^2)}{1a^3 + 1x_ca^2 + 2Kxa + 1Kx_c}
\end{align*}
\]

\[
\begin{align*}
I_{L_{14}}^{(K_x,a)}(K_x,a) &= g_4^{(K_x,a)}(a) \\
V_{L_{14}}^{(K_x,a)}(K_x,a) &= G_4^{(K_x,a)}(a) = \frac{Ka^2 + Kx_a^2 + 2K^2a + K^2x_c}{1a^3 + 1x_ca^2 + 3Kxa + 2Kx_a + 1K}
\end{align*}
\]

\[
\begin{align*}
I_{L_{13}}^{(K_x,a)}(K_x,a) &= g_3^{(K_x,a)}(a) \\
V_{L_{13}}^{(K_x,a)}(K_x,a) &= G_3^{(K_x,a)}(a) = \frac{Ka^2 + Kx_a^2 + 2K^2a + K^2x_c}{1a^3 + 1x_ca^2 + 2Kxa + 1Kx_c}
\end{align*}
\]

\[
\begin{align*}
I_{L_{12}}^{(K_x,a)}(K_x,a) &= g_2^{(K_x,a)}(a) \\
V_{L_{12}}^{(K_x,a)}(K_x,a) &= G_2^{(K_x,a)}(a) = \frac{K(a + Kx_c)}{1a^2 + 1x_ca + 1K}
\end{align*}
\]

\[
\begin{align*}
I_{L_1}^{(K_x,a)}(K_x,a) &= g_1^{(K_x,a)}(a) \\
V_{L_1}^{(K_x,a)}(K_x,a) &= G_1^{(K_x,a)}(a) = \frac{K}{a + 1 + x_c}
\end{align*}
\]

V. TRANSMISSION LINES WITH LOSSES IN SHORT AND OPEN LOAD

In radio frequency telecommunication field, analyzing transmission cables quality is crucial in RF design. Voltage Standing Wave Ratio (VSWR) return losses (RL) and distance to fault (DTF) are the main three ways to check the transmission cable quality and to detect any damage issues. The analysis performed with antenna termination, load termination, short and open load termination. In this paragraph, Fibonacci wave functions FWFs will be determined in both open and short transmission cable termination and compared with recurrent RC-FEC-losses Simulink model order 40 in Fig. 12.

The input impedance or admittance can be found using Pascal’s triangle for the case $R=\Omega; L=\Omega; C=\Omega; r_L = \frac{L}{r_C} = \frac{50\Omega}{0.02\Omega}$. This is a particular case of Pascal’s triangle general form detailed in [1].

Below is an example of $G_{13}(S)$ and $G_{14}(S)$ using Pascal’s triangle in Table III.

For 13th and 13th order RL-FEC-Losses circuit in Fig. 19 is used to determine the corresponding FWFs.

\[
\begin{align*}
\frac{I_{L_1}}{V_{L_1}}^{(K_x,a)}(K_x,a) &= g_1^{(K_x,a)}(a) \\
\frac{V_{L_1}}{I_{L_1}}^{(K_x,a)}(K_x,a) &= G_1^{(K_x,a)}(a) = \frac{K}{a + 1 + x_c}
\end{align*}
\]

\[
\begin{align*}
\frac{I_{L_2}}{V_{L_1}}^{(K_x,a)}(K_x,a) &= g_2^{(K_x,a)}(a) \\
\frac{V_{L_2}}{I_{L_1}}^{(K_x,a)}(K_x,a) &= G_2^{(K_x,a)}(a) = \frac{K(a + Kx_c)}{1a^2 + 1x_ca + 1K}
\end{align*}
\]

\[
\begin{align*}
\frac{I_{L_3}}{V_{L_2}}^{(K_x,a)}(K_x,a) &= g_3^{(K_x,a)}(a) \\
\frac{V_{L_3}}{I_{L_2}}^{(K_x,a)}(K_x,a) &= G_3^{(K_x,a)}(a) = \frac{K(a^2 + Kx^2_c + K^2)}{1a^3 + 1x_ca^2 + 2Kxa + 1Kx_c}
\end{align*}
\]

\[
\begin{align*}
\frac{I_{L_{14}}}{V_{L_{13}}}^{(K_x,a)}(K_x,a) &= g_4^{(K_x,a)}(a) \\
\frac{V_{L_{14}}}{I_{L_{13}}}^{(K_x,a)}(K_x,a) &= G_4^{(K_x,a)}(a) = \frac{Ka^2 + Kx_a^2 + 2K^2a + K^2x_c}{1a^3 + 1x_ca^2 + 3Kxa + 2Kx_a + 1K}
\end{align*}
\]
For RC-FEC-Losses or RL-FEC-Losses, the input impedance or admittance for any order \( n \) and for both short-circuit and open-circuit is as follow.

For short-circuit \(( R = 0 \Omega )\), \( x_c = \infty \) using RC-FEC and \( x_L = 0 \) using RL-FEC-losses. Equations (19), (20) and (21) become

\[
\frac{V}{I_t} = G(\omega = 0) \text{ (} S \text{)} \]

\[
1S^{13} + 12K_{(1)}^{11} + 55K_{(2)}^{4}S^9 + 120K_{(3)}^{2}S^7
+ 126K_{(4)}^{6}S^3 + 56K_{(5)}^{8}S^3 + 7K_{(6)}^8S
\]

\[
= K^* \cdot \frac{I_{o}}{C_{(1)}^{13}} \text{ (} S \text{)} \]

\[
1S^{12} + 11K_{(1)}^{10} + 45K_{(2)}^{2}S^8 + 84K_{(3)}^{3}S^6
+ 70K_{(4)}^{5}S^4 + 21K_{(5)}^{7}S^2 + 1K_{(6)}^6
\]

\[
= K \cdot \frac{I_{o}}{C_{(1)}^{12}} \text{ (} S \text{)} \]

\[
\frac{V}{I_t} = G(\omega = 0) \text{ (} S \text{)} \]

\[
1S^{11} + 10K_{(1)}^{9}S^9 + 36K_{(2)}^{2}S^7
+ 56K_{(3)}^{3}S^5 + 35K_{(4)}^{5}S^3 + 6K_{(5)}^{7}S^3
\]

\[
= K \cdot \frac{I_{o}}{C_{(1)}^{11}} \text{ (} S \text{)} \]

For an open-circuit \(( R = \infty \Omega )\), \( x_c = 0 \) using RC-FEC-Losses and for RL-FEC-Losses \( x_L = \infty \). Equations are determined below.

\[
\frac{V}{I_t} = G(\omega = 0) \text{ (} S \text{)} \]

\[
1S^{13} + 12K_{(1)}^{11} + 55K_{(2)}^{4}S^9 + 120K_{(3)}^{2}S^7
+ 126K_{(4)}^{6}S^3 + 56K_{(5)}^{8}S^3 + 7K_{(6)}^8S
\]

\[
= K^* \cdot \frac{I_{o}}{C_{(1)}^{13}} \text{ (} S \text{)} \]

\[
1S^{12} + 11K_{(1)}^{10} + 45K_{(2)}^{2}S^8 + 84K_{(3)}^{3}S^6
+ 70K_{(4)}^{5}S^4 + 21K_{(5)}^{7}S^2 + 1K_{(6)}^6
\]

\[
= K \cdot \frac{I_{o}}{C_{(1)}^{12}} \text{ (} S \text{)} \]

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\frac{V}{I_t} = G(\omega = 0) \text{ (} S \text{)} \]

\[
1S^{11} + 10K_{(1)}^{9}S^9 + 36K_{(2)}^{2}S^7
+ 56K_{(3)}^{3}S^5 + 35K_{(4)}^{5}S^3 + 6K_{(5)}^{7}S^3
\]

\[
= K \cdot \frac{I_{o}}{C_{(1)}^{11}} \text{ (} S \text{)} \]

Simulations were conducted using general model shown in Fig. 7 and RC-FEC-Losses Simulink model for \( n = 40 \)
\( V(1, x_c = 0, 0) \), \( V(1, x_c = 0, 0, 2) \) are perfectly the same (Fig. 19 and 20).

All current across inductors and all voltages across capacitors are also shown for both FWFs and Simulink model for RC-FEC-Losses order 40 in Fig. 21 and 22.

VI. CONCLUSION

In this paper, a complete Fibonacci wave functions FWFs model that was first applied to an LC ladder network representing lossless transmission line [1] and [2] is extended to LC ladder network presenting losses \(( r_c, r_L) \) to model a transmission line with no distortion subject to Heaviside condition. The general model with losses proposed in this paper helps find automatically all transfer functions, any input impedance or admittance for any recurrent LC network order.

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This research shows the importance of Fibonacci wave functions and their application in modelling recurrent complicated systems. These FWFs model research is still ongoing to model LC ladder network presenting losses \((r_c, r_L)\) with distortion non subject to Heaviside condition.

REFERENCES


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